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# Vectorization

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# What is Vectorization?

- Hardware Perspective: Specialized instructions, registers, or functional units to allow in-core parallelism for operations on arrays (vectors) of data.
- Compiler Perspective: Determine how and when it is possible to express computations in terms of vector instructions
- User Perspective: Determine how to write code in a manner that allows the compiler to deduce that vectorization is possible.



#### **Vectorization: Hardware**

- Goal: parallelize computations over vector arrays
- SIMD: Single Instruction Multiple Data
- Many instances of a single operation executing simultaneously
  - Late '90s present, commodity CPUs (x86, x64, PowerPC, etc)
  - Small vectors, few cycles per instruction
  - Newer CPUs (post Sandy Bridge) can pipeline some SIMD instructions as well – best of both worlds.



# **Vectorization via SIMD: Motivation**

- CPU speeds reach a plateau
  - Power limitations!
  - Many "slow" transistors more efficient than fewer "fast" transistors
- Process improvements make physical space cheap
  - Moore's law, 2x every 18-24 months
  - Easy to add more "stuff"
- One solution: More cores
  - First dual core Intel CPUs appear in 2005
  - Increasing in number rapidly (e.g. 8 in Stampede, 61 on MIC)
- Another Solution: More FPU units per core vector operations
  - First appeared on a Pentium with MMX in 1996
  - Increasing in vector width rapidly (e.g. 512-bit [8 doubles]) on MIC



#### **Vectorization via SIMD: History**

Year	Registers	Instruc	Instruction Set	
~1997	80-bit	MMX	Integer SIMD (in x87 registers)	
~1999	128-bit	SSE1	SP FP SIMD (xMM0-8)	
~2001	128-bit	SSE2	DP FP SIMD (xMM0-8)	
	128-bit	SSEx		
~2010	256-bit	AVX	DP FP SIMD (yMM0-16)	
~2012	512-bit	IMCI	(MIC)	
~2015	512-bit	AVX-51	.2 (Skylake?)	



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#### **Vector Registers**





#### Speed

- True SIMD parallelism Can take 1 cycle per floating point computation on all values in a vector register.
  - Exception: Slow operations like division, square roots
- Speedup (compared to no vector) proportional to vector width
  - 128-bit SSE 2x double, 4x single
  - 256-bit AVX 4x double, 8x single
  - 512-bit MIC 8x double, 16x single
- Hypothetical AVX example: 8 cores/CPU \* 4 doubles/vector \* 2.0 GHz = 64 Gflops/CPU DP
- Gets even better with FMA (fused multiply add), a=a+(b\*c). Multiply and add in the same clock cycle (Haswell+).



#### Speed

- Clearly memory bandwidth is potential issue, we'll explore this later
  - Poor cache utilization, alignment, memory latency all detract from ideal
- SIMD is parallel, so Amdahl's law is in effect!
  - Serial/scalar portions of code or CPU are limiting factors
  - Theoretical speedup is only a ceiling





#### **User Perspective**

Let's take a step back – how can we leverage this power

- Program in assembly
  - Ultimate performance potential, but only for the brave
- Program in intrinsics
  - Step up from assembly, useful but risky
- Let the compiler figure it out
  - Relatively "easy" for user, "challenging" for compiler
  - Less expressive languages like C make compiler's job more difficult
  - Compiler may need some hand holding.
- Link to an optimized library that does the actual work
  - e.g. Intel MKL, written by people who know all the tricks.
  - Get benefits "for free" when running on supported platform



#### **Vector-aware coding**

- Know what makes vectorizable at all
  - "for" loops (in C) or "do" loops (in fortran) that meet certain constraints
- Know where vectorization will help
- Evaluate compiler output
  - Is it really vectorizing where you think it should?
- Evaluate execution performance
  - Compare to theoretical speedup
- Know data access patterns to maximize efficiency
- Implement fixes: directives, compilation flags, and code changes
  - Remove constructs that make vectorization impossible/impractical
  - Encourage/force vectorization when compiler doesn't, but should
  - Better memory access patterns



# Writing Vector Loops

- Basic requirements of vectorizable loops:
  - Countable at runtime
    - Number of loop iterations is known before loop executes
    - No conditional termination (break statements)
  - Have single control flow
    - No Switch statements
    - 'if' statements are allowable when they can be implemented as masked assignments
  - Must be the innermost loop if nested
    - Compiler may reverse loop order as an optimization!
  - No function calls
    - Basic math is allowed: pow(), sqrt(), sin(), etc
    - Some Inline functions allowed



# **Conceptualizing Compiler Vectorization**

- Think of vectorization in terms of loop unrolling
  - Unroll N interactions of loop, where N elements of data array fit into vector register

```
for (i=0; i<N;i++) {
    a[i]=b[i]+c[i];
}
Load b(i..i+3)
Load c(i..i+3)
Operate b+c->a
for (i=0; i<N;i+=4) {
    a[i+0]=b[i+0]+c[i+0];
    a[i+1]=b[i+1]+c[i+1];
    a[i+2]=b[i+2]+c[i+2];
    a[i+3]=b[i+3]+c[i+3];
}</pre>
```



# **Compiling Vector loops**

- Intel Compiler:
  - Vectorization starts at optimization level -02
  - Will default to SSE instructions and 128-bit vector width
    - use –xAVX to use AVX and 256-bit vector width. Only runs on newer CPUs
  - Can embed SSE and AVX instructions in the same binary with -axAVX
    - Will run AVX on CPUs with AVX support, SSE otherwise
  - -vec-report=<n> for a vectorization report
- GCC
  - Vectorization is disabled by default, regardless of optimization level
  - Need -ftree-vectorize flag, combined with optimization > -02
  - SSE by default, -mavx -march=corei7-avx for AVX
  - -ftree-vectorizer-verbose for a vectorization report



# Lab: Simple Vectorization

In this lab you will

- Use the Intel compiler to create vectorized with non-vectorized code
- Compare the performance of vectorized vs non-vectorized code
- Compare performance with different vector widths.
- Take an initial look at compiler vectorization reports
- Bonus: What is the vector efficiency (% vector instructions) of the test code? Using Amdal's law P = (1/(S-1))/((1/(n-1))) where P is % parallel (e.g. % vectorized), S is speedup, n is vector length in number of floats/doubles



# Lab: Simple Vectorization

	Compile Options	Time	Speedup
Host CPU	-no-vec –O3	.67s	1x
	-03	.37s	1.8x
	-O3 –xAVX (or –xhost)	.25s	2.7x
MIC	Compile Options	Time	Speedup
	-no-vec -mmic -O3	13.22s	1x
	-mmic -O3	2.78s	4.8x

Notes:

- One MIC thread can only use 50% of a core
- Amdahl's law for 90% vectorized predicts (1x, 1.8x, 3x, 4.7x)



#### **Challenge: Loop Dependencies**

- Vectorization changes the order of computation compared to sequential case
- Compiler must be able to prove that vectorization will produce correct result.
- Need to consider independence of *unrolled* loop operations depends on vector width
- Compiler performs dependency analysis



# Loop Dependencies: Read After Write

Consider the loop:

belleter the heap: a = {0,1,2,3,4} b = {5,6,7,8,9} for ( i=1; i<N; i++) a[i] = a[i-1] + b[i];

#### Applying each operation sequentially: $a[1] = a[0] + b[1] \rightarrow a[1] = 0 + 6 \rightarrow a[1] = 6$ $a[2] = a[1] + b[2] \rightarrow a[2] = 6 + 7 \rightarrow a[2] = 13$ $a[3] = a[2] + b[3] \rightarrow a[3] = 13 + 8 \rightarrow a[3] = 21$ $a[4] = a[3] + b[4] \rightarrow a[4] = 21 + 9 \rightarrow a[4] = 30$

a = {0, 6, 13, 21, 30}



# Loop Dependencies: Read After Write

Consider the loop:

belleter the height a= {0,1,2,3,4} b = {5,6,7,8,9} for ( i=1; i<N; i++) a[i] = a[i-1] + b[i];

Applying each operation sequentially:

 $\begin{array}{l} a[1] = a[0] + b[1] \rightarrow a[1] = 0 + 6 \rightarrow a[1] = 6 \\ a[2] = a[1] + b[2] \rightarrow a[2] = 6 + 7 \rightarrow a[2] = 13 \\ a[3] = a[2] + b[3] \rightarrow a[3] = 13 + 8 \rightarrow a[3] = 21 \\ a[4] = a[3] + b[4] \rightarrow a[4] = 21 + 9 \rightarrow a[4] = 30 \end{array}$ 

a = {0, 6, 13, 21, 30}



# Loop Dependencies: Read After Write

Now let's try vector operations: a= {0,1,2,3,4} b = {5,6,7,8,9} for ( i=1; i<N; i++) a[i] = a[i-1] + b[i];

```
Applying vector operations, i=\{1,2,3,4\}:

a[i-1] = \{0,1,2,3\} (load)

b[i] = \{6,7,8,9\} (load)

\{0,1,2,3\} + \{6,7,8,9\} = \{6, 8, 10, 12\} (operate)

a[i] = \{6, 8, 10, 12\} (store)
```

```
a = {0, 6, 8, 10, 12} ≠ {0, 6, 13, 21, 30} NOT VECTORIZABLE
```



# **Loop Dependencies: Write after Read**

Consider the loop:

belleter the heap: a = {0,1,2,3,4} b = {5,6,7,8,9} for ( i=0; i<N; i++) a[i] = a[i+1] + b[i];

#### Applying each operation sequentially: $a[0] = a[1] + b[0] \rightarrow a[0] = 1 + 5 \rightarrow a[0] = 6$ $a[1] = a[2] + b[1] \rightarrow a[1] = 2 + 6 \rightarrow a[1] = 8$ $a[2] = a[3] + b[2] \rightarrow a[2] = 3 + 7 \rightarrow a[2] = 10$ $a[3] = a[4] + b[3] \rightarrow a[3] = 4 + 8 \rightarrow a[3] = 12$

a = {6, 8, 10, 12, 4}



# Loop Dependencies: Write after Read

Now let's try vector operations: a= {0,1,2,3,4} b = {5,6,7,8,9} for ( i=0; i<N; i++) a[i] = a[i+1] + b[i];

```
Applying vector operations, i=\{1,2,3,4\}:

a[i+1] = \{1,2,3,4\} (load)

b[i] = \{5,6,7,8\} (load)

\{1,2,3,4\} + \{5,6,7,8\} = \{6, 8, 10, 12\} (operate)

a[i] = \{6, 8, 10, 12\} (store)
```

```
a = {0, 6, 8, 10, 12} = {0, 6, 8, 10, 12} VECTORIZABLE
```



#### **Loop Dependencies**

- Read After Write
  - Also called "flow" dependency
  - Variable written first, then read
  - Not vectorizable

- Write after Read
  - Also called "anti" dependency
  - Variable read first, then written
  - vectorizable

for( i=0; i<N-1; i++)
a[i] = a[i+1] + b[i];</pre>



#### **Loop Dependencies**

- Read after Read
  - Not really a dependency
  - Vectorizable

for( i=0; i<N; i++)
 a[i] = b[i%2] + c[i];</pre>

- Write after Write
  - a.k.a "output" dependency
  - Variable written, then re-written
  - Not vectorizable

# for( i=0; i<N; i++) a[i%2] = b[i] + c[i];</pre>



# Loop Dependencies: Aliasing

- In C, pointers can hide data dependencies!
  - Memory regions they point to may overlap
- Is this safe?:

- .. Not if we give it the arguments compute (a, a+1, c);
  - Effectively, b is really a[i-1]  $\rightarrow$  Read after Write dependency
- Compilers can usually cope, add bounds checking tests (overhead)



#### **Vectorization Reports**

- Shows which loops are or are not vectorized, and why
- Intel: -vec-report=<n>
  - 0: None
  - 1: Lists vectorized loops
  - 2: Lists loops not vectorized, with explanation
  - 3: Outputs additional dependency information
  - 4: Lists loops not vectorized, without explanation
  - 5: Lists loops not vectorized, with dependency information
- Reports are essential for determining where the compiler finds a dependency
- Compiler is conservative, you need to go back and verify that there really is a dependency.



# Loop Dependencies: Vectorization Hints

- Compiler must prove there is no data dependency that will affect correctness of result
- Sometimes, this is impossible
  - e.g. unknown index offset, complicated use of pointers
- Intel compiler solution: IVDEP (Ignore Vector DEPendencies) hint.
  - Tells compiler "Assume there are no dependencies"

```
subroutine
vec1(s1,M,N,x)
...
int N,double s1,int M,
int N,double *x) {
...
!DEC$ IVDEP
do i = 1,N
x(i) = x(i+M) + s1
end dovoid vec1(double s1,int M,
int N,double *x) {
...
#pragma IVDEP
for(i=0;i<N;i++) x[i]=x[i+M]+s1;
```



# **Compiler hints affecting vectorization**

- For Intel compiler only
- Affect whether loop is vectorized or not
- #pragma ivdep
  - Assume no dependencies.
  - Compiler may vectorize loops that it would otherwise think are not vectorizable
- #pragma vector always
  - Always vectorize if technically possible to do so.
  - Overrides compiler's decision to not vectorize based upon cost
- #pragma novector
  - Do not vectorize



# Loop Dependencies: Language Constructs

- C99 introduced 'restrict' keyword to language
  - Instructs compiler to assume addresses will not overlap, ever

• May need compiler flags to use, e.g. -restrict, -std=c99



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# **Cache and Alignment**



- Optimal vectorization requires concerns beyond SIMD unit!
  - Registers: Alignment of data on 128, 256 bit boundaries
  - Cache: Cache is fast, memory is slow
  - Memory: Sequential access much faster than random/strided



#### **Strided access**

- Fastest usage pattern is "stride 1": perfectly sequential
- Best performance when CPU can load L1 cache from memory in bulk, sequential manner
- Stride 1 constructs:
  - Iterating Structs of arrays vs arrays of structs
  - Multi dimensional array:
    - Fortran: stride 1 on "inner" dimension
    - C/C++: Stride 1 on "outer" dimension



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#### **Strided access**

- Striding through memory reduces effective memory bandwidth!
  - For DP, roughly 1-stride/8
- Worse than non-aligned access. Lots of memory operations to populate a cache line, vector register



#### Cost of Memory-Strided Summation



# **Diagnosing Cache and Memory deficiencies**

- Obviously bad stride patterns may prevent vectorization at all:
  - In vector report: "vectorization possible but seems inefficient"
- Otherwise, may be difficult to detect
  - No obvious assembly instructions, other than a proliferation of loads and stores
  - Vectorization performance farther away from ideal than expected
- Profiling tools can help
  - PerfExpert (available at TACC)
  - Visualize CPU cycle waste spent in data access (L1 cache miss, TLB misses, etc)



#### Conclusion

- Vectorization occurs in tight loops "automatically" by the compiler
- Need to know where vectorization should occur, and verify that compiler is doing that.
- Need to know if a compiler's failure to vectorize is legitimate
  - Fix code if so, use #pragma if not
- Need to be aware of caching and data access issues
  - Very fast vector units need to be well fed.